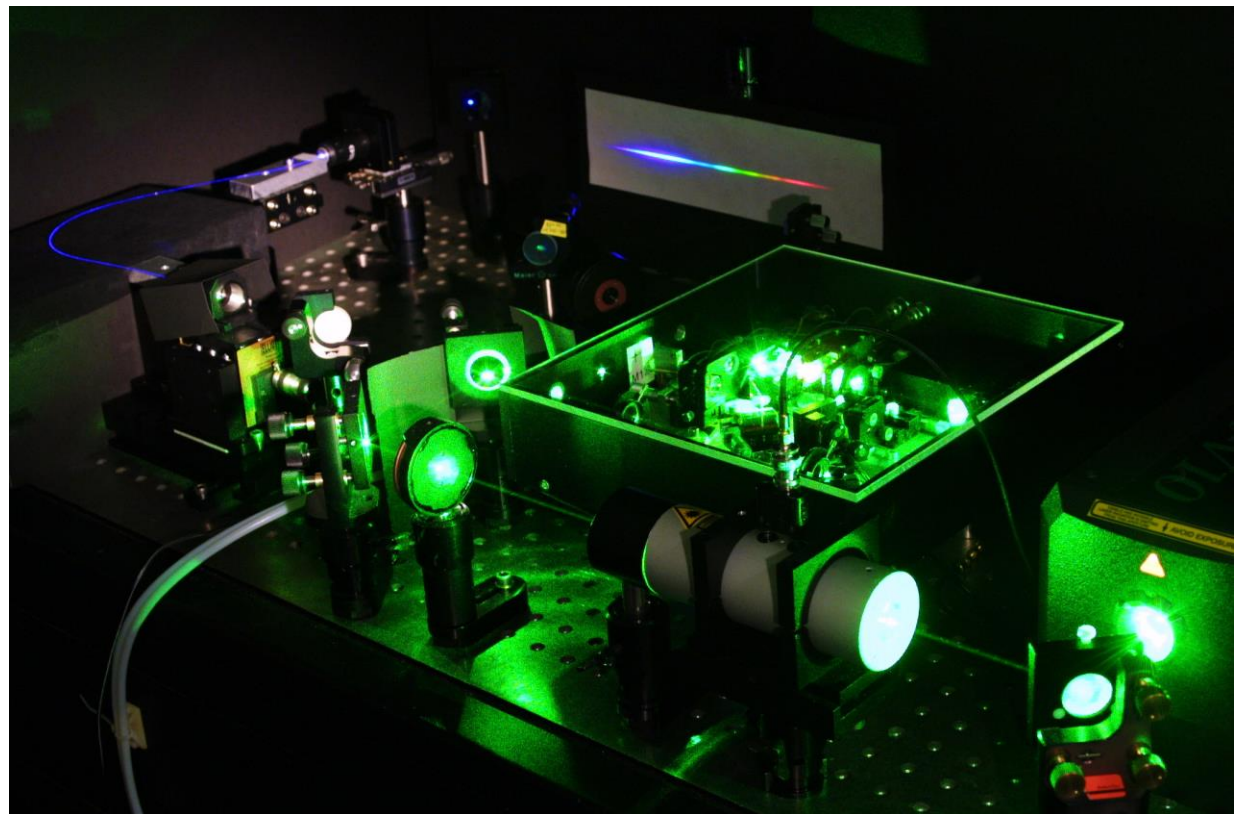
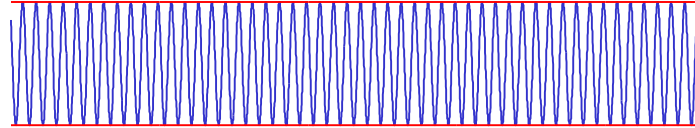


Measuring the Frequency of Light with Mode Locked Lasers

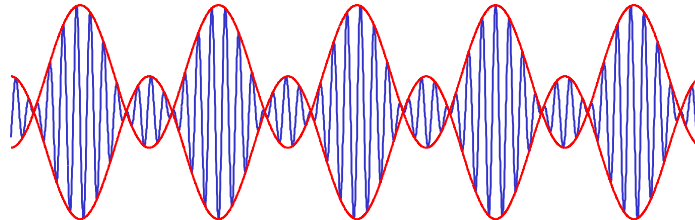


Locking the Cavity Modes of a Laser

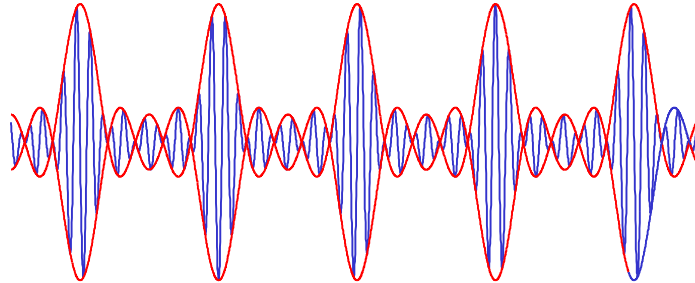
single mode :



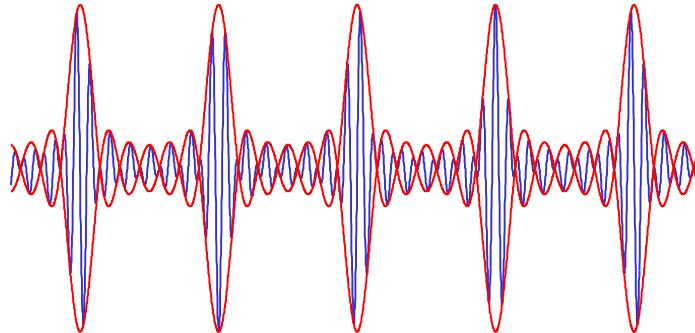
3 modes :



5 modes :



7 modes :



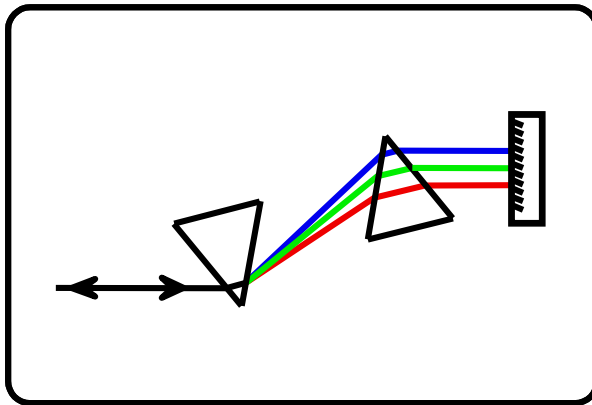
...

The Soliton Laser

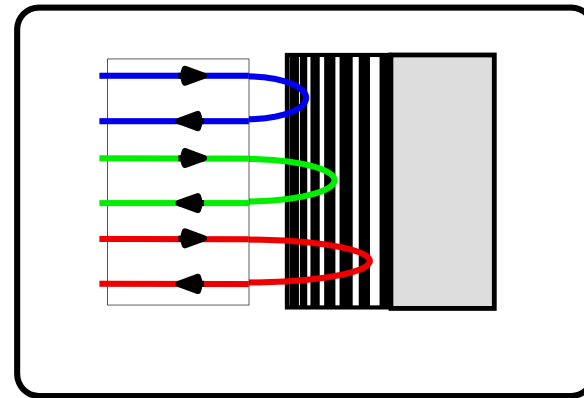
The effect of group velocity dispersion (GVD) and self phase modulation (SPM) on the pulse reshaping cancel in a soliton.

- SPM: laser crystal $n(I) = n_0 + I(t) n_2$ with $n_2 > 0$
- GVD: prism pairs and/or chirped mirrors $d^2\tau/dk^2 < 0$

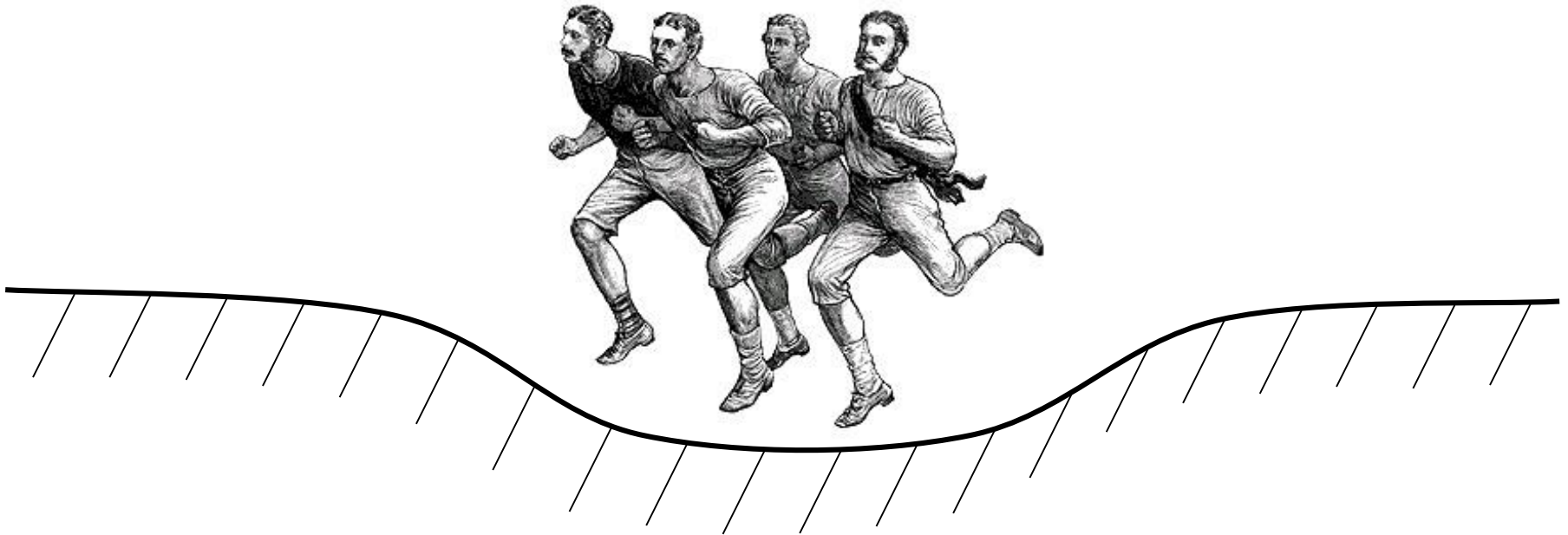
prism pair



chirped mirror

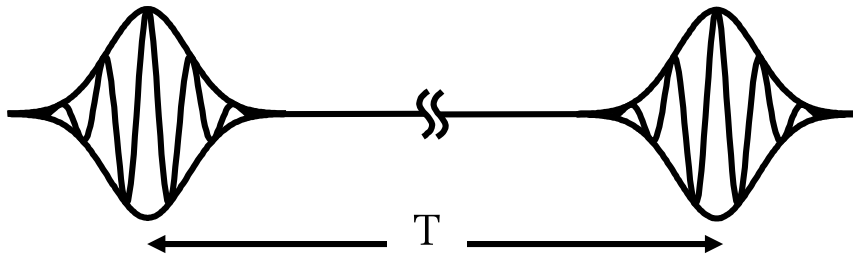


Mechanical Soliton: Runners on a Soft Surface

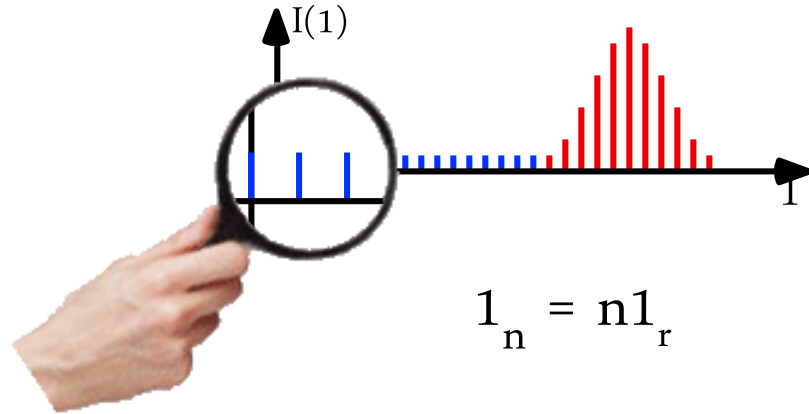


Carrier Envelope Phase of the Pulses

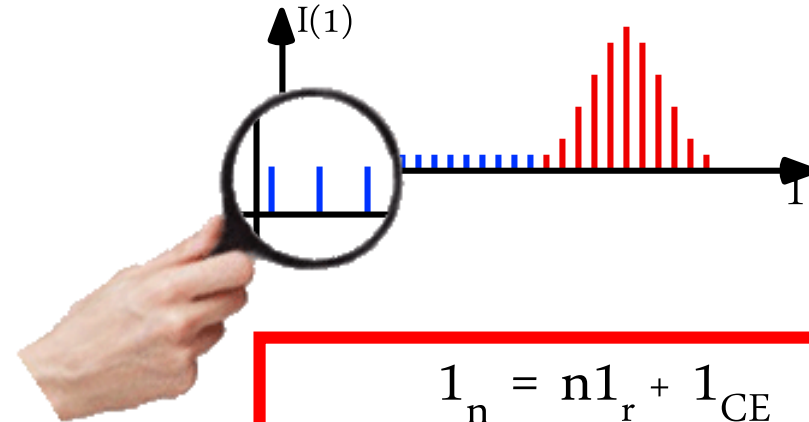
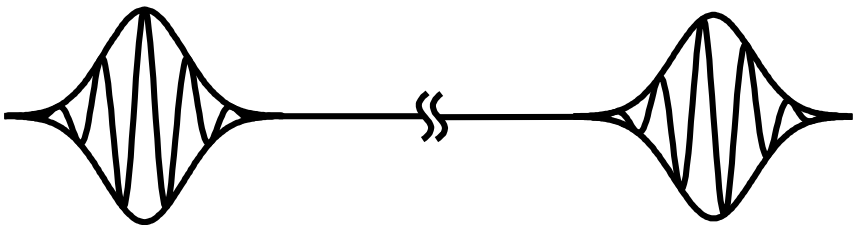
group velocity = phase velocity



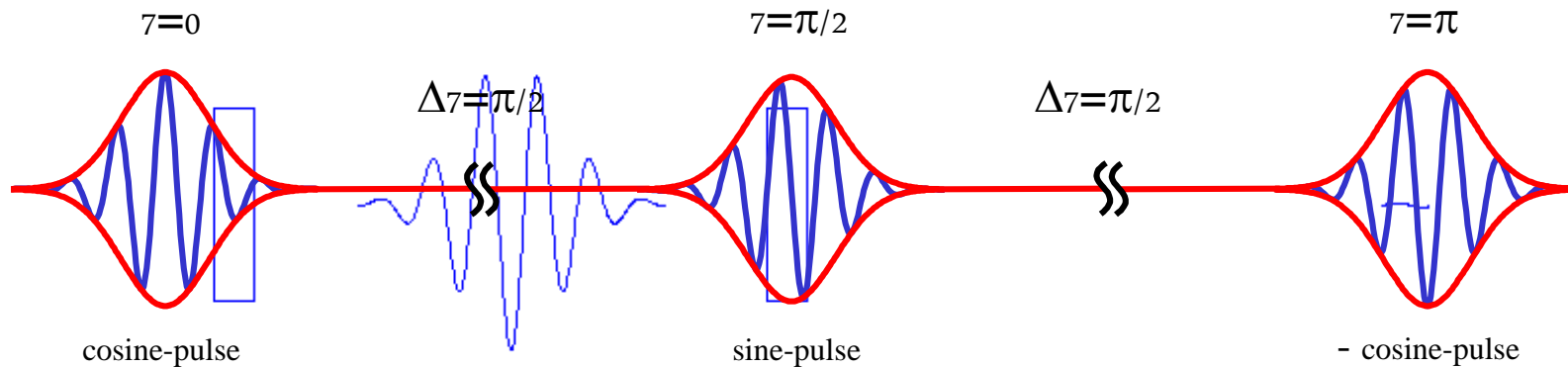
repetition rate: $1_r = 2\pi/T$



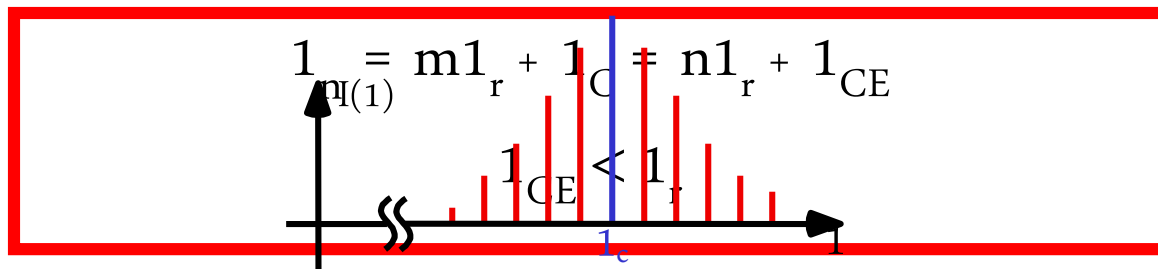
group velocity \neq phase velocity



Carrier Envelope Offset Frequency

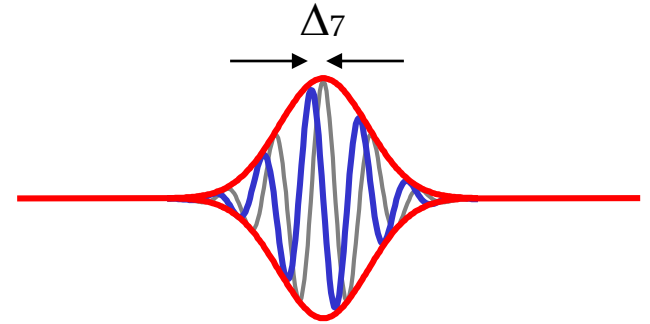


$$E(t) = A(t) e^{-i\omega_c t} = \sum_{m=-\infty}^{+\infty} A_m e^{-im\omega_r t - i\omega_c t}$$



Pulse-to-Pulse Carrier Envelope Phase Slippage

$$E(t) = \sum_{n=-\infty}^{+\infty} A_n e^{-in\omega_r t - i\omega_{CE} t}$$



$$E(t+T) = \sum_{n=-\infty}^{+\infty} A_n e^{-in\omega_r(t+T) - i\omega_{CE}(t+T)}$$

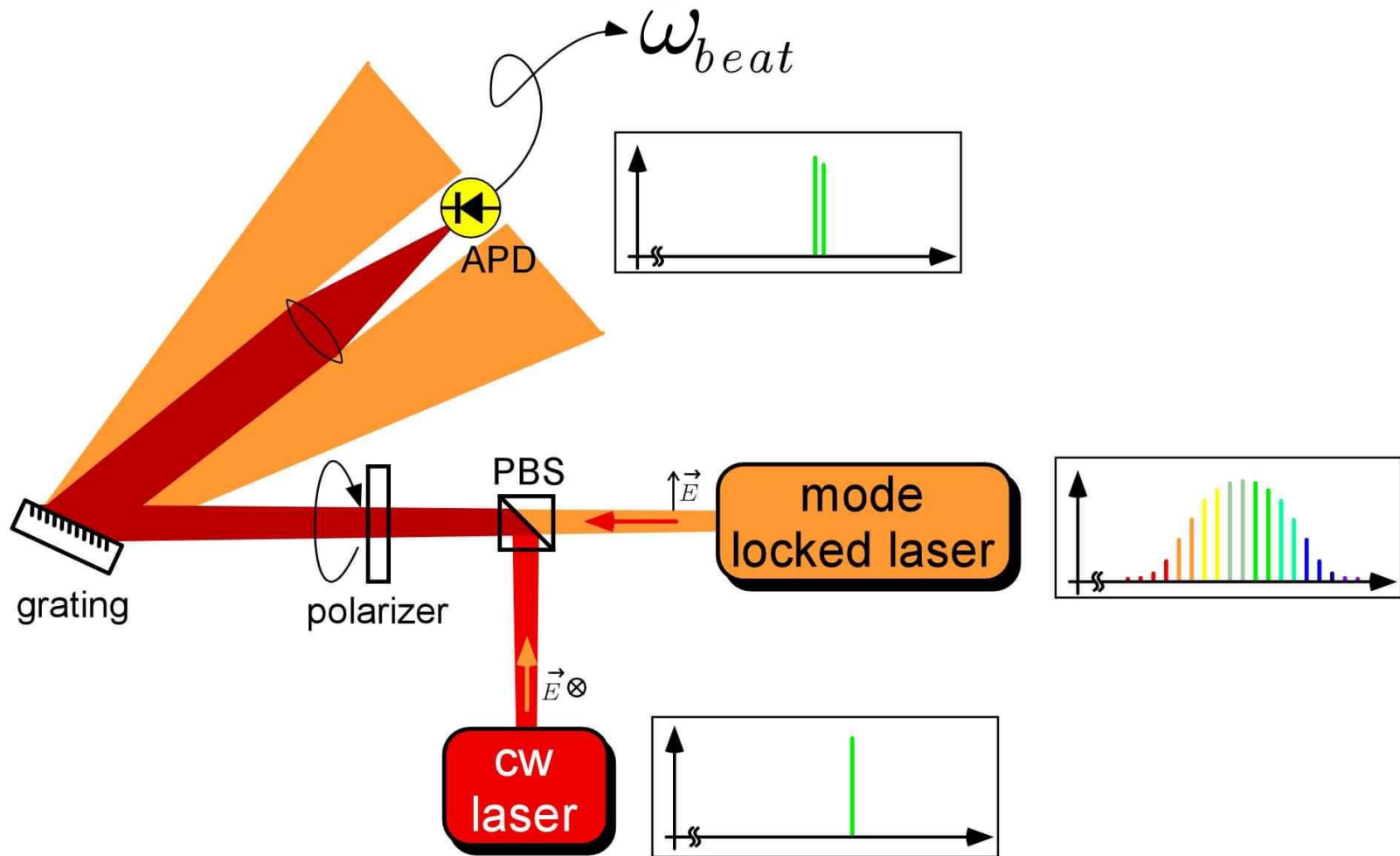
$$= E(t) e^{-i\Delta\phi}$$



$$\Delta\phi = 2\pi \omega_{CE} / \omega_r$$

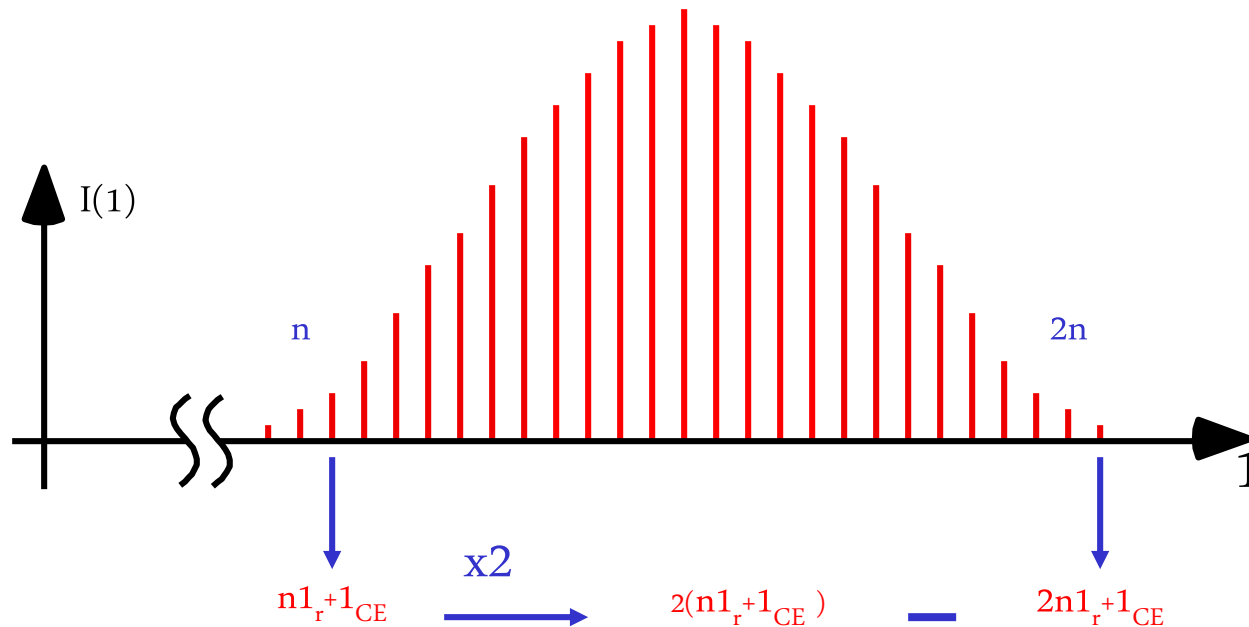
$$\omega_{CE} = \Delta\phi / T$$

Selecting a Single Mode from the Comb



Measuring the Carrier-Envelope Phase Slippage

it is simple to detect 1_{CE} of an octave wide frequency comb:



$$1_{CE} = 2(n1_r + 1_{CE}) - (2n1_r + 1_{CE})$$

Controlling the Frequency Comb

depends on the cavity length

$$1_n = n1_r + 1_{CE}$$

depends on the pump power



we can measure **and** control

$$1_r = 2\pi/T \text{ and } 1_{CE} = \Delta\omega/T$$

Optical Frequency Counter

locked to a Cs atomic clock

$$\nu_n = n\nu_r + \nu_{\text{CE}}$$

every mode can be used for
optical frequency measurement

Optical Prescaler (Frequency Divider)

locked to an optical reference



$$1_n = n1_r + 1_{CE}$$

locked to a fraction of 1_r



$$= (n + 1/k) 1_r$$



countable clock output

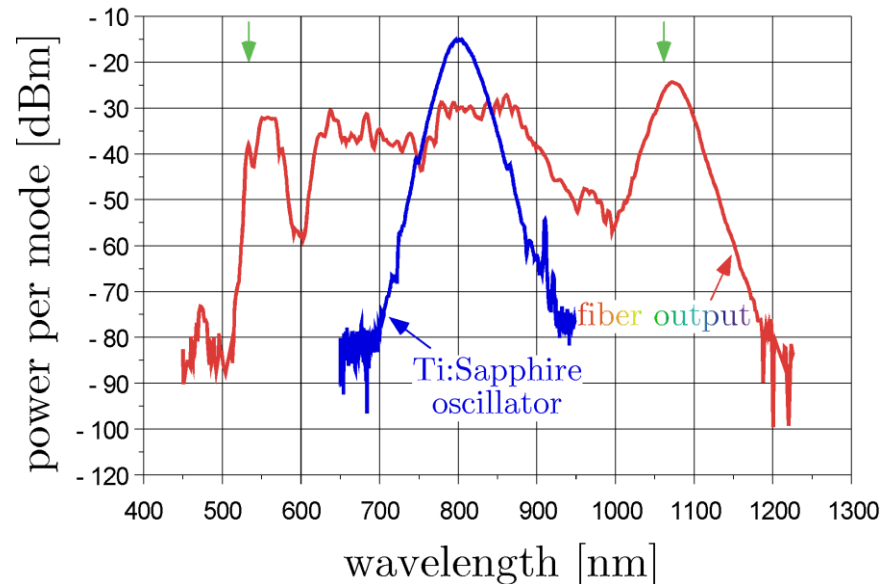
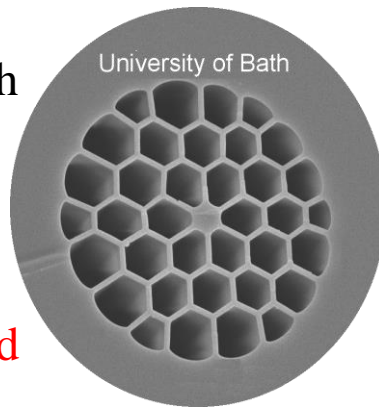
Generating an Octave Spanning Comb

self phase modulation: $n(I) = n_0 + I(t) n_2$ with $I(t) \sim |A(t)|^2$

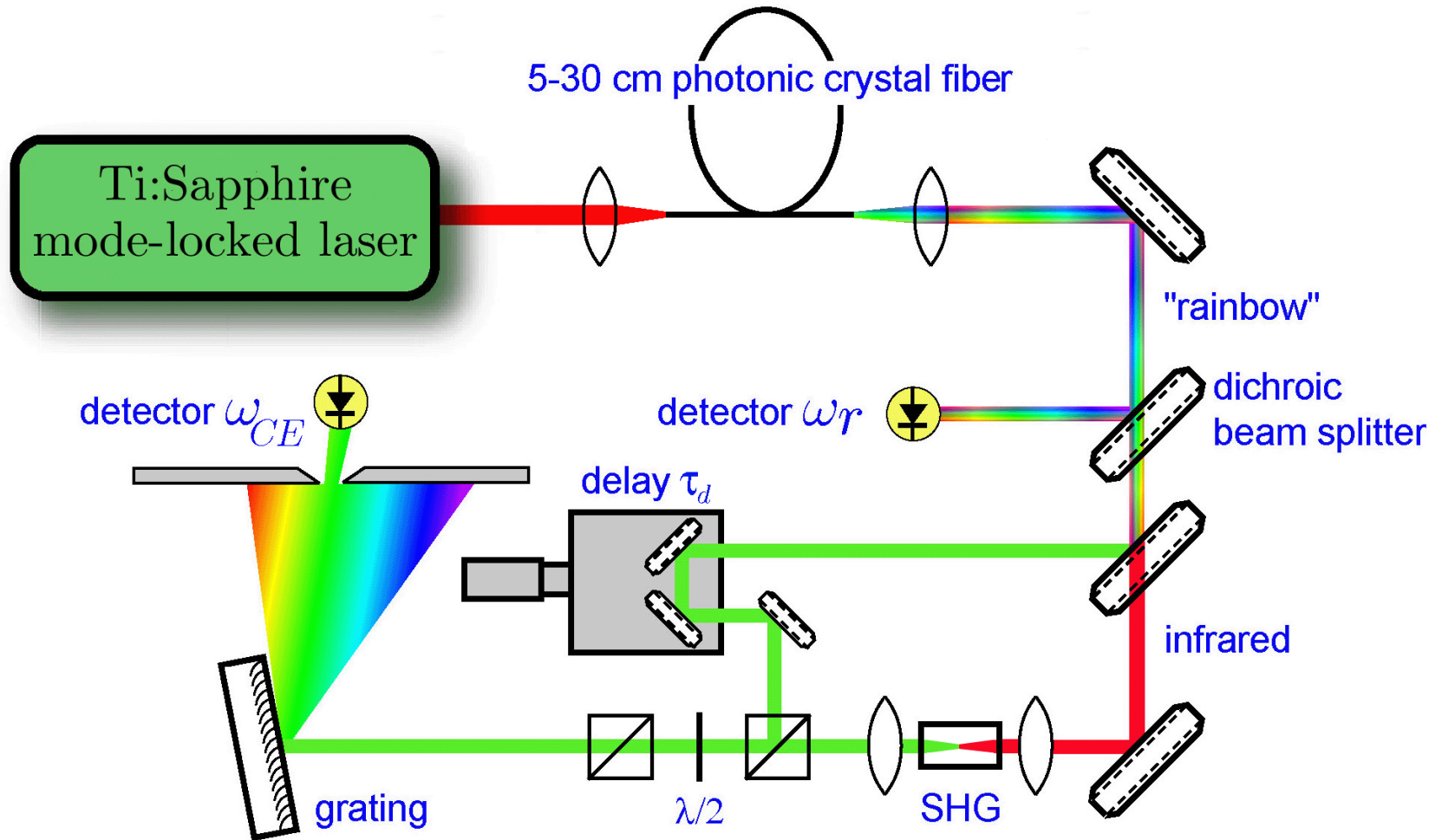
non-linear phase shift after propagating the length l : $\Phi_{NL}(t) = - I(t) n_2 l/c$

→ extra frequencies: $\dot{\Phi}_{NL}(t) = - \dot{I}(t) n_2 l/c$

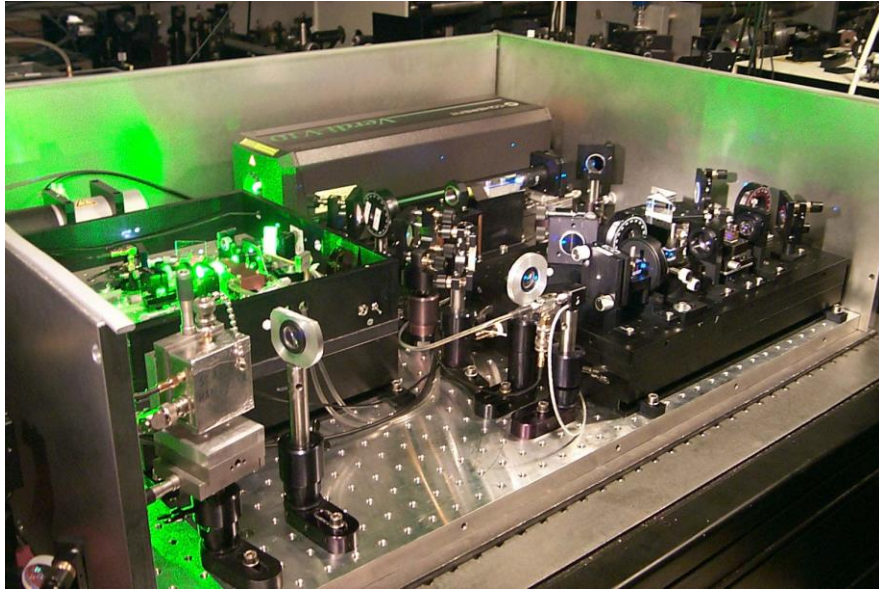
William Wadsworth
Jonathan Knight
Tim Birks
Phillip Russell
U. of Bath England



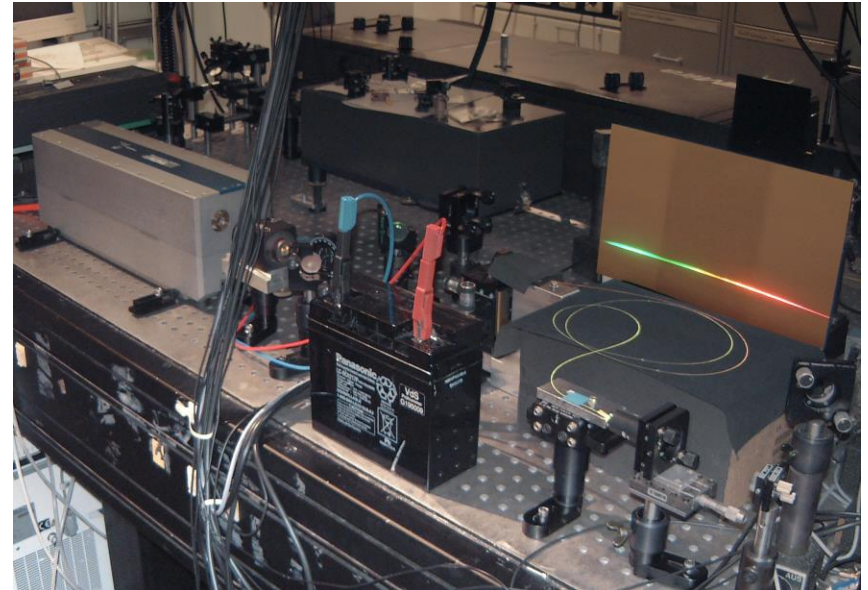
Self Referencing the Frequency Comb



Optical Synthesizer

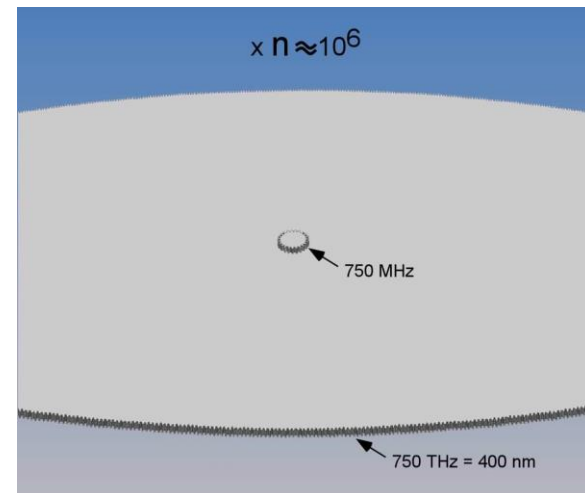
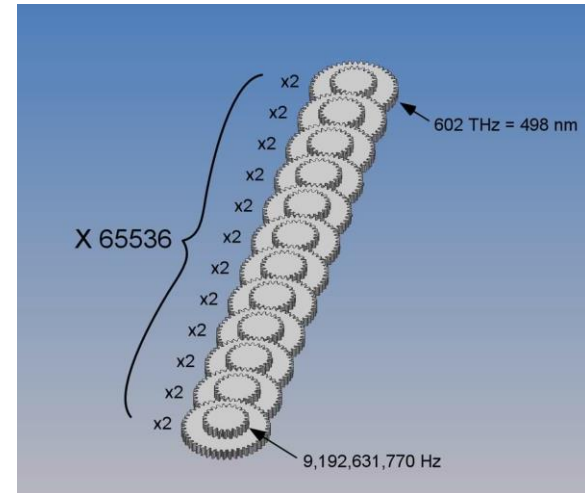
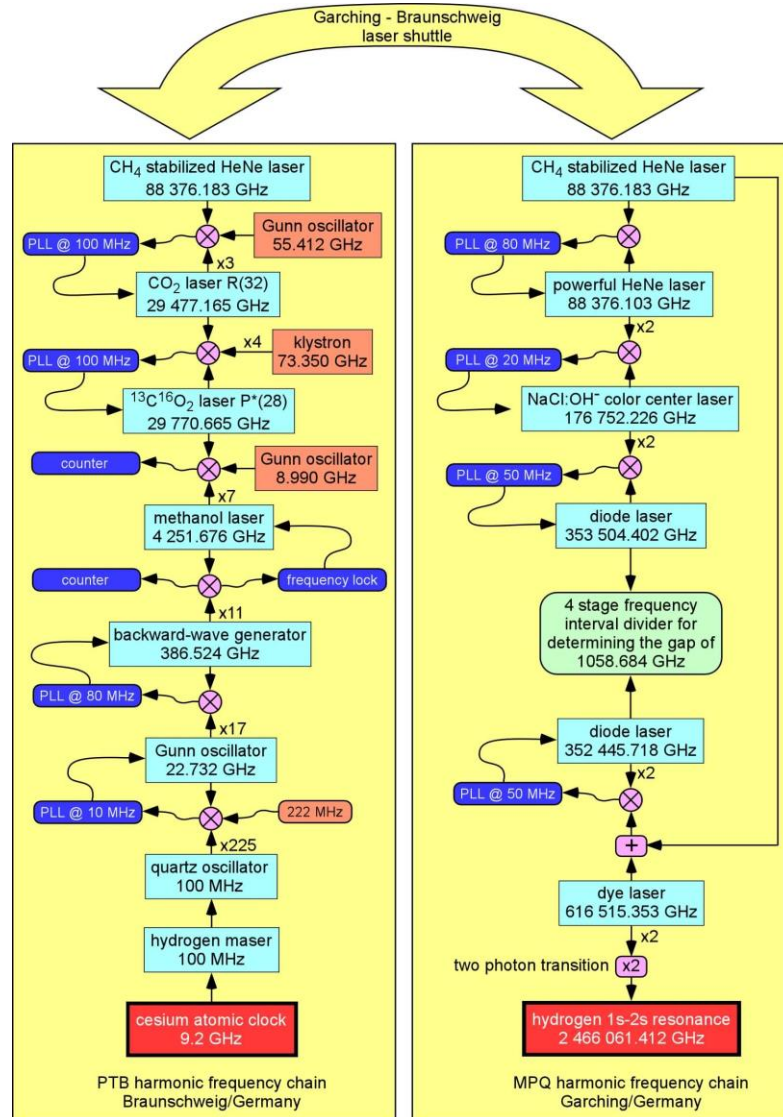


Based on a 650 MHz Ti:sapphire ring laser (GigaOptics).



Based on a Cr:LiSAF laser made at RTWH Aachen by P.Russbült, K.Gäbel and R.Poprave.

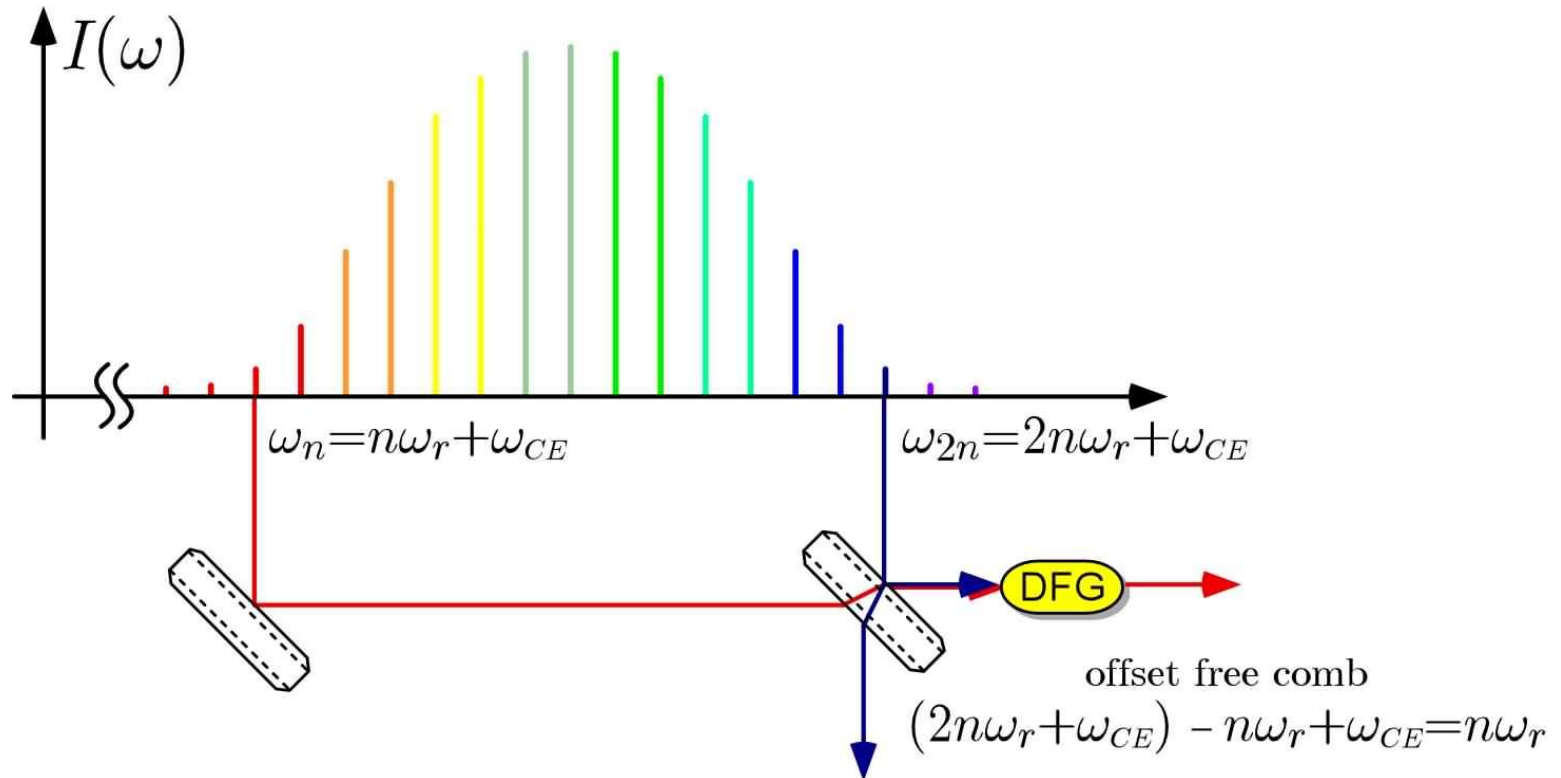
Harmonic Frequency Chains vs Optical Synthesizers



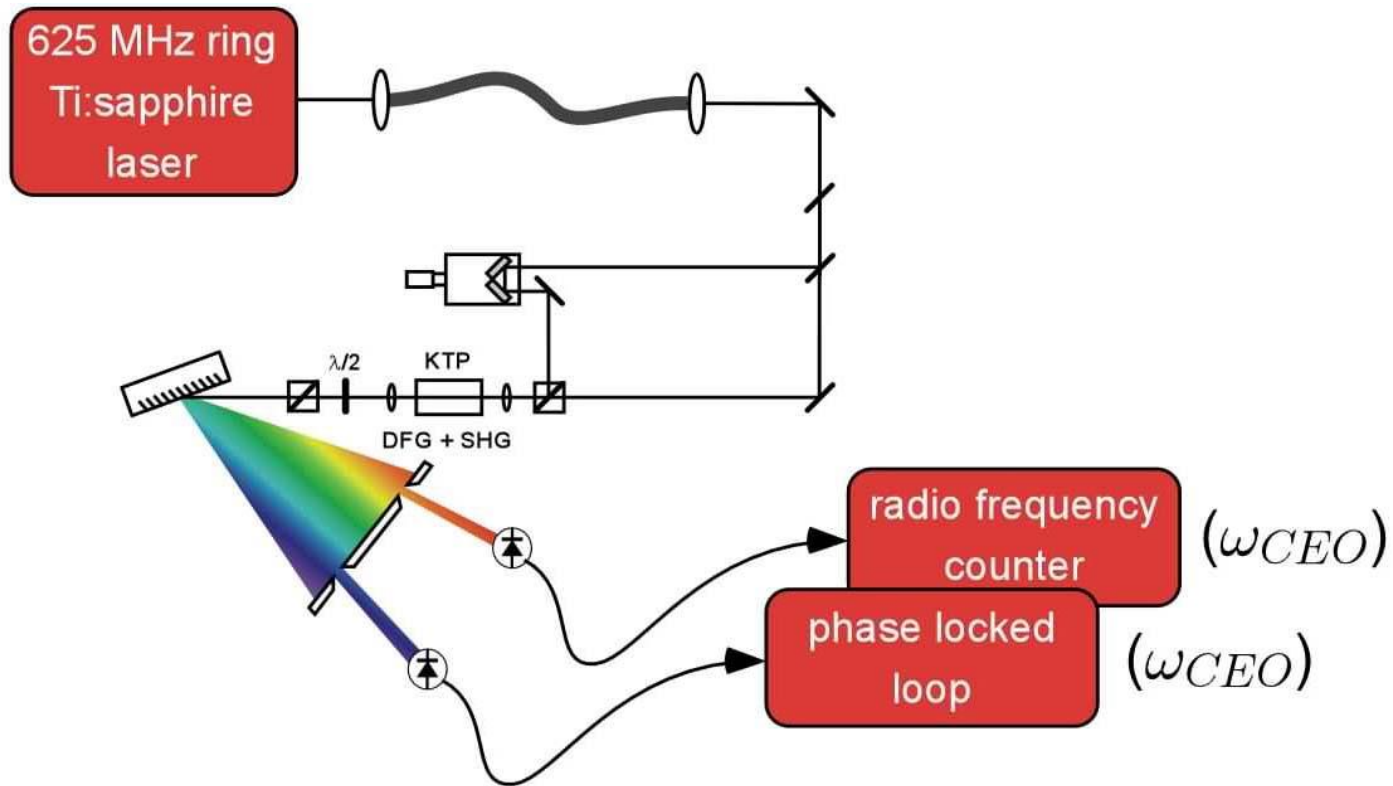
Adjusting the transmission ratio by selecting n:

$$1_n = n1_r + 1_{\text{CEO}}$$

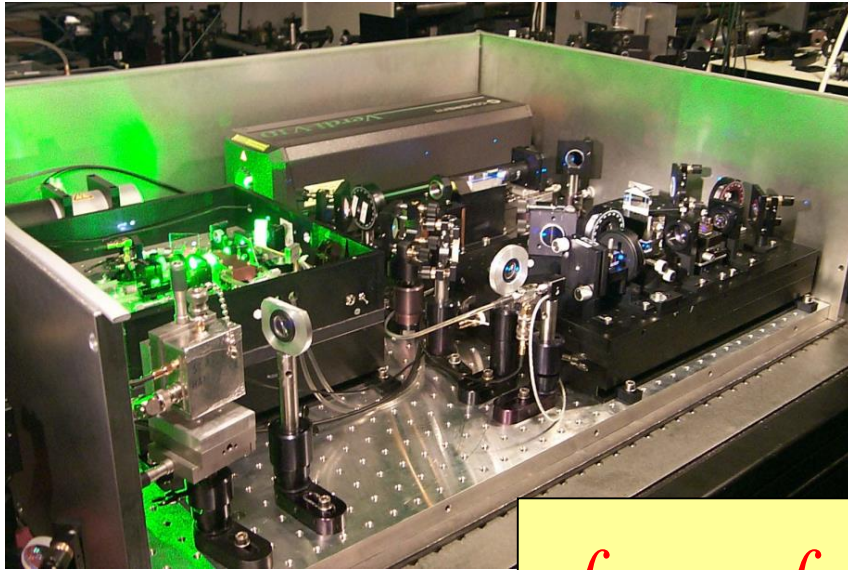
Self Differencing the Comb



Testing the Self-Differenced Comb



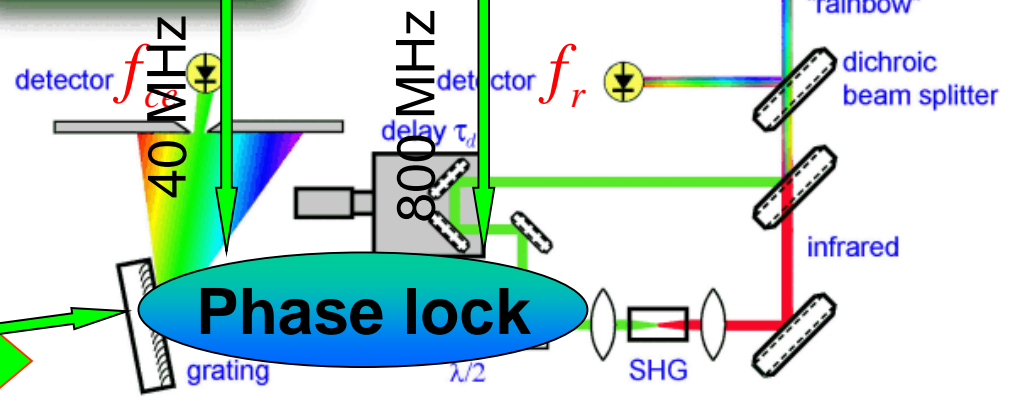
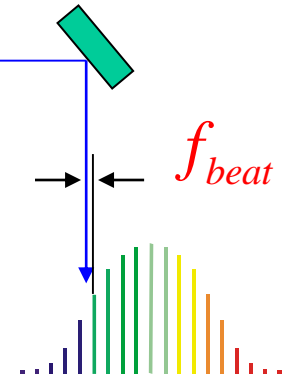
Frequency Measurement



486 nm laser

770 664

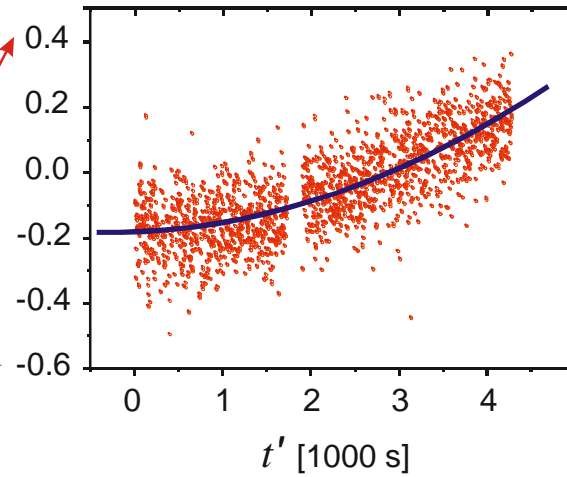
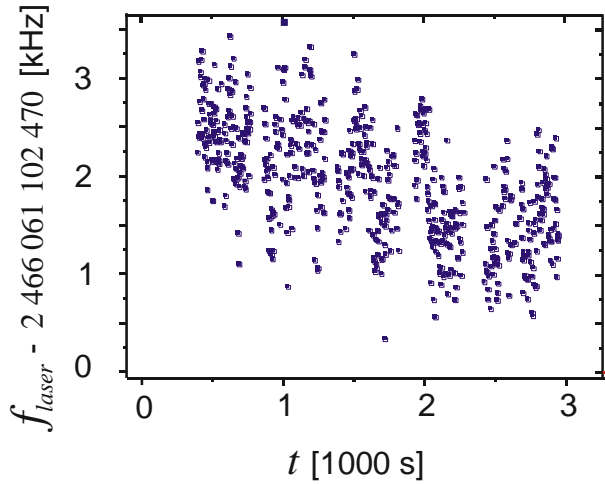
$$f_{laser} = f_{beat} + f_{ce} + N \cdot f_r$$



Primary Reference

Laser frequency measurement example

HP5701A
clock



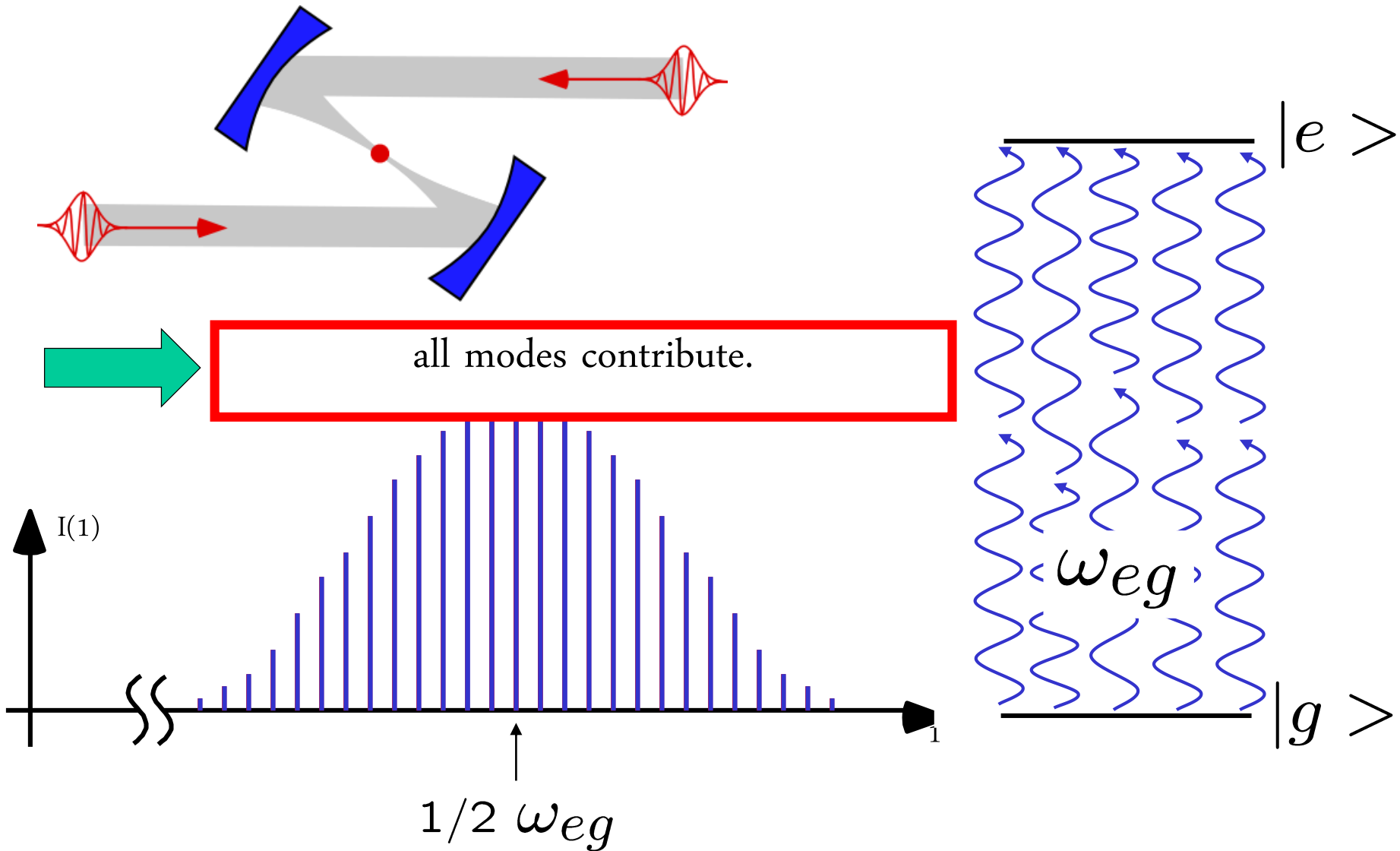
FOM

Other Applications



- Precision Spectroscopy
- Time Domain: Stabilization of the CE phase

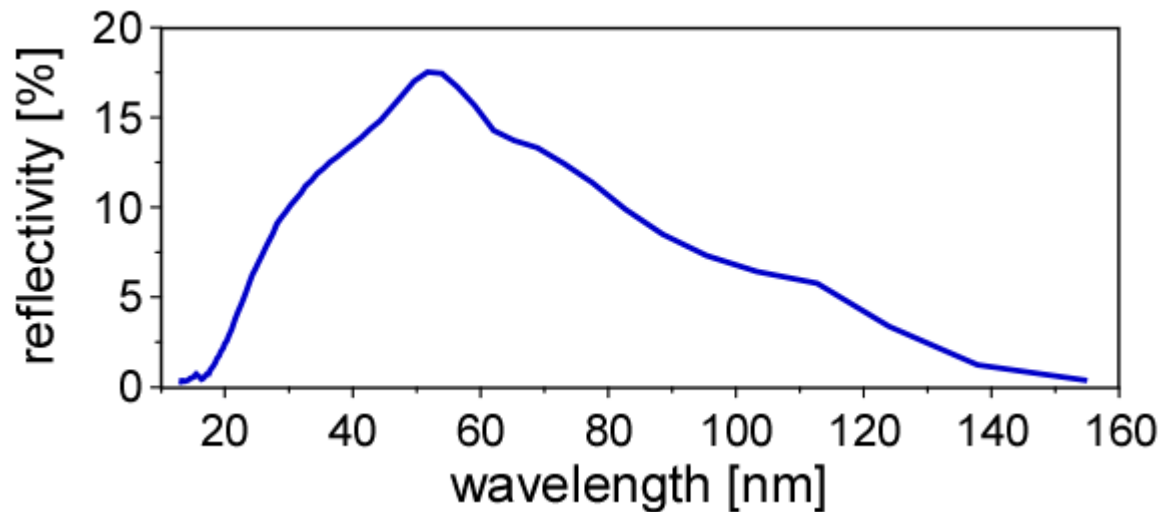
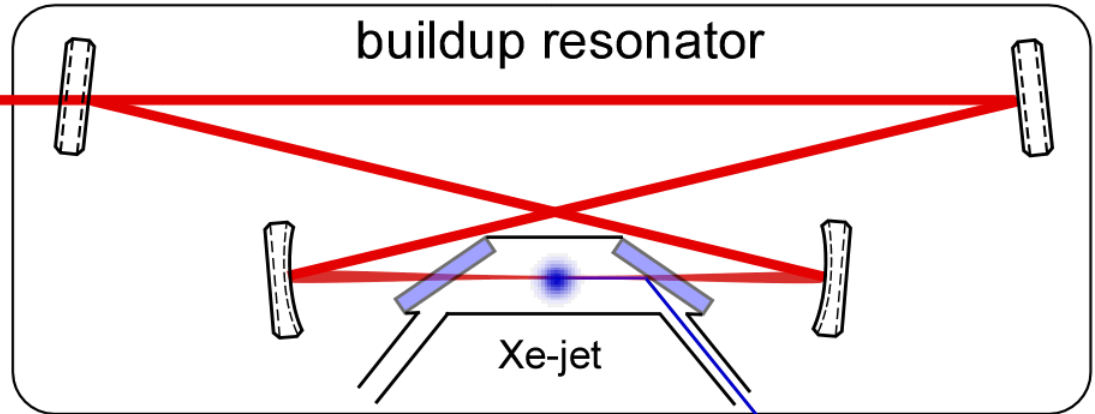
Doing Spectroscopy with the Comb



HHGs with 114 MHz Repetition Rate

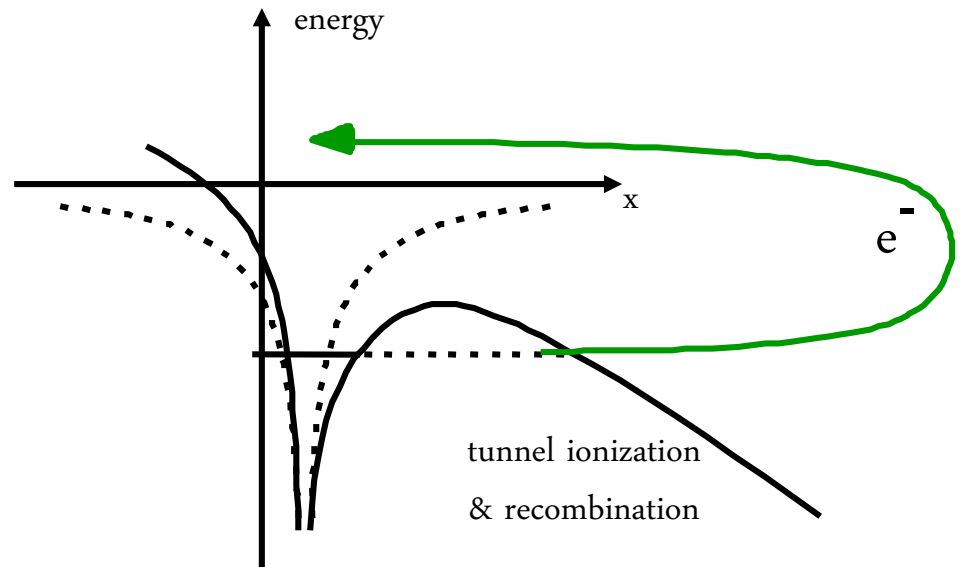
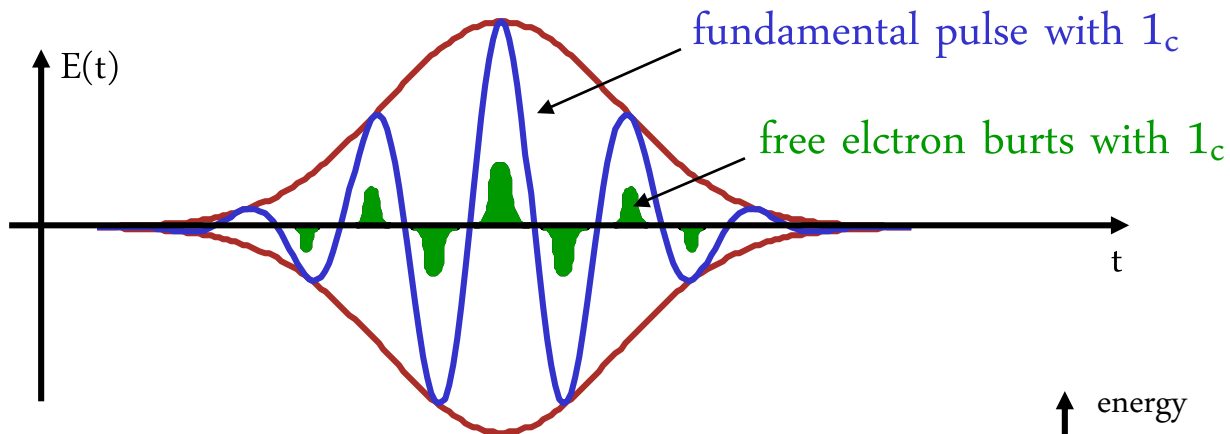
focal spot $\sim 5.3 \mu\text{m}$ $1/e$ diameter $\sim 5.5 \times 10^{13} \text{ W/cm}^2$

20 fs mode locked
Ti:Sapphire laser



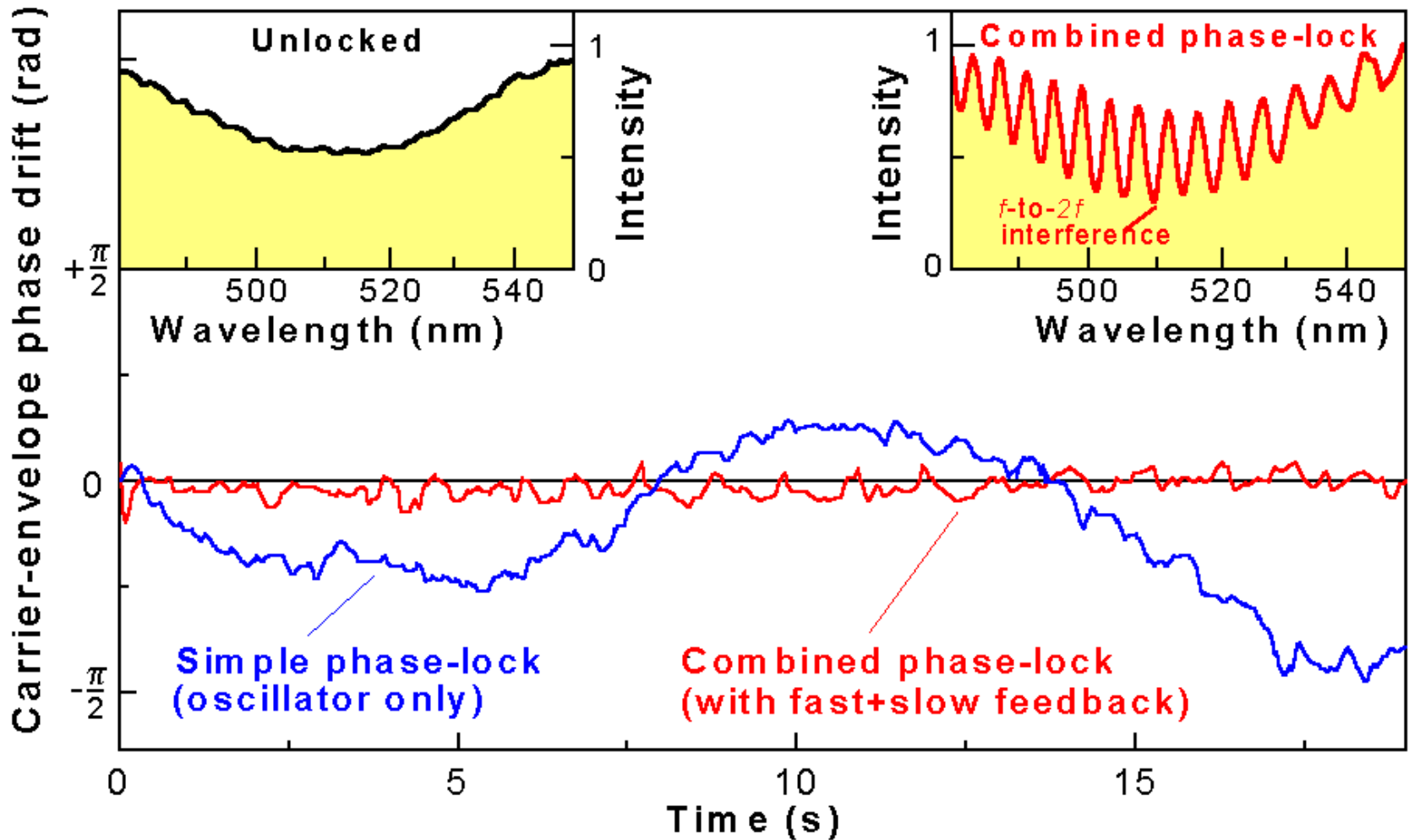
XUV output

High Harmonics Generation (HHG)

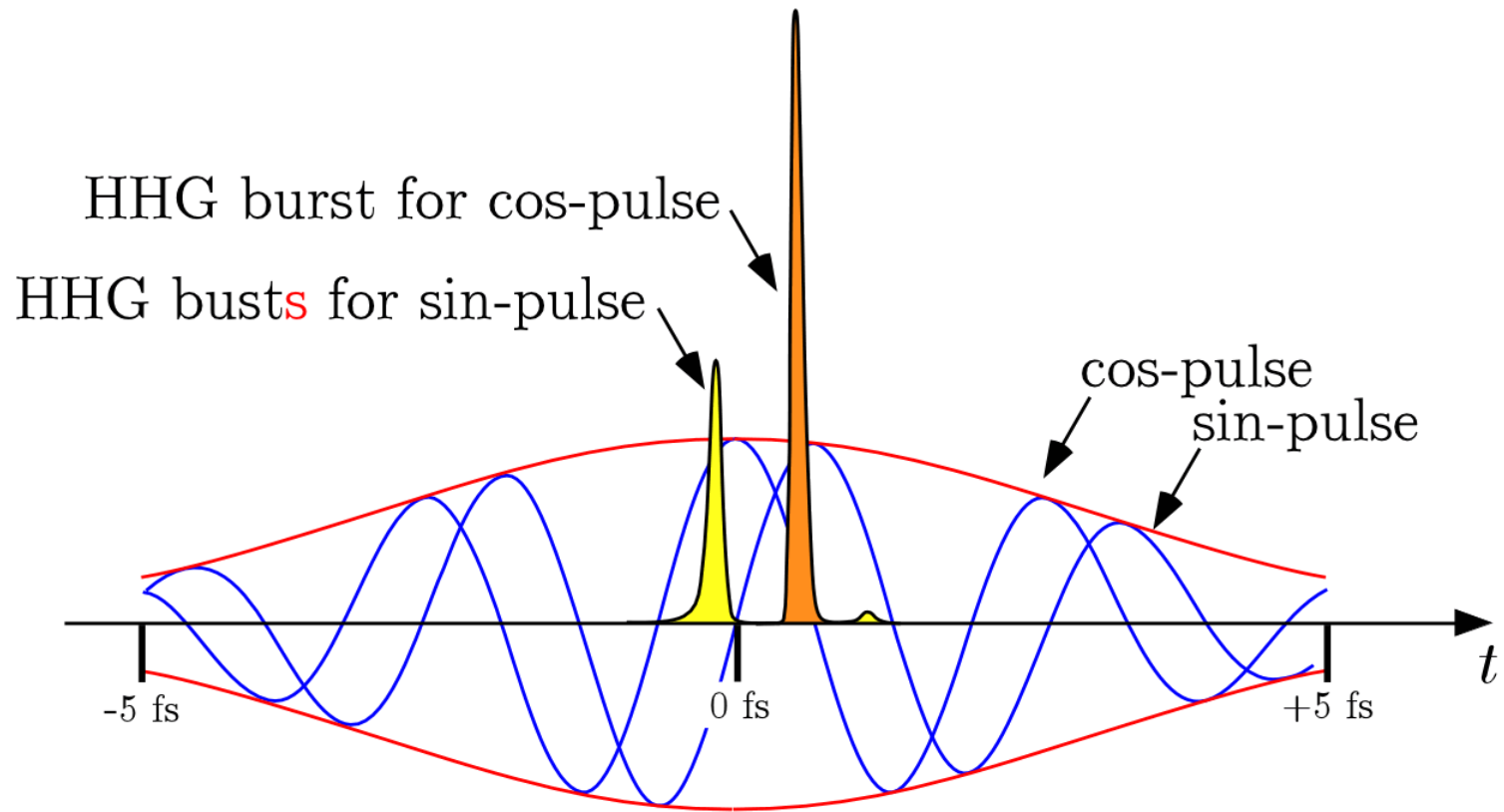


- free electrons emit HHG's
- only odd orders created
- HHG vanish for small elliptic polarization
- very short pulses make HHG's merge

Stabilizing the CE Phase of Intense Pulses



Phase Sensitive High Harmonic Generation



calculated HHG intensity @ 3.2nm

Phase Sensitive High Harmonic Generation

